## IB Math Applications and Interpretations Summer Assignment

Course Title: IB Math: Applications and Interpretations (formerly IB Math Studies)
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Purpose of Assignment: The following summer assignment is designed to prepare you for the forthcoming IB Math course. This summer assignment contains content that has already been covered in previous Algebra classes but must be mastered before entering the course. The assignment is designed to allow you to review the material previously covered in math courses so that you will be well prepared with several ideas that occur throughout the IB Math course.

Estimated time to complete the assignment: On an average it will take $4-6$ hours to complete the assignment.

## Algebra Review Worksheets

All work must be done neatly on your own paper. Make sure each page of your work is labeled with the corresponding Worksheet Number and Topic Name. Answers to problems must be circled to facilitate grading. Most importantly, the work should be neat! Remember this assignment is not collected for a grade, but only students who complete the assignment will be able to retake the quiz.

You will need your own graphing calculator (TI-84 is recommended) for this course.
A quiz will be given over the material covered on the review worksheets. The summer assignment quiz will occur the $2^{\text {nd }}$ week of school

Thank you.
Have a great summer! Looking forward to meeting you.
Mrs. MacLeod

## Worksheet 1 - Exponent Properties

Review:

1. $a^{n} * a^{m}=a^{n+m}$
2. $\left(a^{n}\right)^{m}=a^{n m}$
3. $\frac{a^{n}}{a^{m}}=a^{n-m}$
4. $a^{0}=1(a \neq 0)$
5. $a^{-n}=\frac{1}{a^{n}}$
6. $(a b)^{n}=a^{n} b^{n}$

Practice:

1. $x^{2} \cdot x^{3}$
2. $\left(2 k^{3}\right)\left(-4 k^{4}\right)\left(3 k^{-2}\right)$
3. $\left(-2 x^{3}\right)^{2}$
4. $-\left(2 x^{3}\right)^{2}$
5. $\left(-2 x^{2}\right)^{3}$
6. $-\left(2 x^{2}\right)^{3}$
7. $x^{-3}$
8. $4 x^{-3}$
9. $\frac{3}{x^{-2}}$
10. $\frac{-5}{x^{-4}}$
11. $\frac{x^{8}}{x^{2}}$
12. $\frac{x^{3}}{x^{6}}$
13. $\frac{x^{-3}}{4 x^{5}}$
14. $\frac{-10 x^{15}}{5 x^{-3}}$
15. $x^{2} \cdot x^{-2}$
16. $x^{0}$
17. $\left(\frac{4 x^{2}}{5 y}\right)^{3}$
18. $\left(3 y^{2}\right)\left(2 y^{21}\right)$
19. $\left(4 x^{3} y^{2}\right)(-3 x y)$
20. $\left(-2 s t^{5}\right)\left(-4 s t^{-3}\right)$
21. $\left(5 a^{2} b^{3}\right)\left(a^{-2} b\right)$
22. $\left(-\frac{a^{-3}}{3 a^{-1} b}\right)^{4}$
23. $\frac{3}{4 d} \cdot \frac{(2 d)^{4}}{c^{3}}$
24. $y^{0}\left(8 x^{6} y^{-3}\right)^{-2}$
25. $\left(5 r^{5}\right)^{3} \cdot r^{-2}$

## Worksheet \#2 - Trigonometry Review

## Review:

Make sure your calculator is in degree mode. We saw in Geometry that $\sin (A N G L E)=$ RATIO . The trigonometry functions relate sides of of a right triangle. You probably saw the mnemonic:

## SOH CAH TOA

$\sin =\frac{\text { opposite }}{\text { hypotenuse }} \quad \cos =\frac{\text { adjacent }}{\text { hypotenuse }} \quad \tan =\frac{\text { opposite }}{\text { adjacent }}$

Ex 1. Solve for the variables


$$
\tan 54^{\circ}=\frac{y}{705} \quad \cos 54^{\circ}=\frac{705}{x}
$$

$$
705 * \tan 54^{\circ}=y x * \cos 54^{\circ}=705
$$

$$
x=\frac{705}{\cos 54^{\circ}}
$$

Now type into the calculator

Ex 2. Solve for the angle T

$\tan T=\frac{23}{17}$
$T=\left(\frac{23}{17}\right)$

Now type into calculator

## Angles of Elevation and Depression:

Angle of Elevation - The angle that looks upwards from a horizontal between two objects
Angle of Depression - The angle that looks downwards from a horizontal between two objects.


## Practice:

Questions 1-9: Find the value of the variable to the nearest tenth.
1.

2.

21
3.

6.


8.



Questions 10-13: Accurately draw a picture representing the problem and answer the question.
10. A building casts a shadow 40 feet long when the sun's angle of elevation is $58^{8}$. Find the height of the building to the nearest foot.
11. A forest ranger watches for fires from a look-out tower built on a high hill. The site of the tower is 740 m above most of the surrounding land, and the tower itself is 24 m tall. If the ranger sights a fire at an angle of $7^{\boxtimes}$ (hint: it is an angle of depression), how far, to the nearest meter, is the fire from the top of the tower?
12. When the sun's angle of elevation is $42^{\square}$, a tree casts a shadow 17 m long. How tall is the tree to the nearest meter?
13. The angle of depression from the top of a tower to a point $A$ is $23^{8}$. The distance from $A$ to the base, $B$, of the tower is 80 m . How tall is the tower to the nearest meter?

## Worksheet \#3 - Systems of Equations

## Review:

## Substitution

Example:

$$
\left\{\begin{array}{l}
y=3 x+2 \\
x+2 y=11
\end{array}\right.
$$

Since we have $\mathrm{y}=$, replace y in the $2^{\text {nd }}$ equation to get: $\quad x+2(3 x+2)=11$
Now we distribute and combine like terms:
$x+6 x+4=11 \rightarrow 7 x+4=11$

Solve for x :
$7 x=7 ; \quad x=1$
Now substitute back into $y=3 x+2$ to find $y$ : $y=3(1)+1=4$

Write your answer:

## Linear Combinations (Elimination):

Example: $\quad\left\{\begin{array}{l}6 x+5 y=19 \\ 2 x+3 y=5\end{array}\right.$
The goal is to add (or subtract) the two equations so one variable is removed.

Multiply the $2^{\text {nd }}$ equation by -3 to get:

$$
6 x+5 y=19-6 x-9 y=-15
$$

Add the two equations together:

$$
-4 y=-4
$$

Solve for y :

Substitute into either original equation to get x :
$y=1$
$2 x+3(1)=5$
$2 x=2$
$x=1$
***Note sometimes you need to multiply both equations by a number***

## Graphing:

Isolate the variable $y$ in each equation and type those equation in the $y=$ feature on your graphing calculator. Then hit the 2ND button then the TRACE button then option \#5: intersect.

Practice: Solve by any method, but make sure you understand all three methods.

1. $\left\{\begin{array}{l}y=3 x+4 \\ y=-2 x-1\end{array} \quad\right.$ 2. $\left\{\begin{array}{l}9 x+2 y=39 \\ 6 x+13 y=-9\end{array}\right.$
2. $\left\{\begin{array}{l}8 x-7 y=-3 \\ 6 x-5 y=-1\end{array}\right.$
3. $\left\{\begin{array}{l}x+y=3 \\ x-y=5\end{array}\right.$
4. $\left\{\begin{array}{l}y=2 x-4 \\ -6 x+3 y=-12\end{array}\right.$
5. $\left\{\begin{array}{l}3 x-2 y=3 \\ -x+y=1\end{array}\right.$
6. $\left\{\begin{array}{l}2 x+y=-15 \\ y-5 x=6\end{array}\right.$
7. $\quad\left\{\begin{array}{l}x+y=-1 \\ -2 x+y=-7\end{array}\right.$

$$
\begin{aligned}
& y=x^{2}-3 \\
& x^{2}+y^{2}=9
\end{aligned}
$$

$$
\begin{aligned}
& y^{2}-x^{2}+3 y=26 \\
& x^{2}+2 y^{2}=34
\end{aligned}
$$

$$
\begin{aligned}
& y^{2}=10-6 x^{2} \\
& 4 y^{2}=40-2 x^{2}
\end{aligned}
$$

12. 

## Worksheet \#4 - Domain and Inverses

## Review:

Domain - the possible set of input values (often associated with the $x$-axis)

Range - the set of output values (often associated with the $y$-axis)
Relation - a set of ordered pairs
Function - a relation where each input value corresponds to exactly one output value. (this means for every $x$-value there is only one possible $y$-value).

Inverses - reverses or undoes the effect of a relation/function.

IB expects you to know that if the point $(a, b)$ is on a relation, then the point $(b, a)$ is on its inverse. This is what you saw in Algebra two when you switched the $x$ and $y$ values, then solved for $y$ to create the inverse. Since we are switching the input and output values, this means that the domain of the function will be the range of its inverse.

Notation: The inverse of a function $f(x)$ is written as $f^{-1}(x)$, and $f(a)=b$, then $f^{-1}(b)=a$.
This also means that the inverse is a reflection in the line $\mathrm{y}=\mathrm{x}$ of the original.

## Example:

1. If $f(-10)=5$, then find $f^{-1}(5)$.
$f(-10)=5$ represents the point $(-10,5)$
The inverse of this point is $(5,-10)$
This means $f^{-1}(5)=-10$.

## Practice:

1. a. Is the graph a function?
b. What is the domain?
c. What is the range?
d. On the same graph, sketch the inverse.
e. What is the domain of the inverse?

2. a. Is the graph a function?
b. What is the domain?
c. What is the range?
d. On the same graph, sketch the inverse.
e. What is the domain of the inverse?

3. a. Is the graph a function?
b. What is the domain?
c. What is the range?
d. On a new graph, sketch the inverse.
e. What is the domain of the inverse?
f. Is the inverse a function?

4. a. Is the graph a function?
b. What is the domain?
c. What is the range?
d. On a new graph, sketch the inverse.
e. What is the domain of the inverse?
f. Is the inverse a function?


## Worksheet \#5 - Quadratics

## Review:

The standard form of a quadratic function is:

$$
y=a x^{2}+b x+c
$$

$\star$ The parabola opens up if a $>0$ and opens down if a $<0$
$\star$ The axis of symmetry is the vertical line $x=\frac{-b}{2 a}$
$\star$ The vertex lies on the axis of symmetry. $\left(\frac{-b}{2 a}, f\left(\frac{-b}{2 a}\right)\right)$

The Quadratic Formula:

$$
x=\frac{-b \pm \sqrt{b^{2}-4 a c}}{2 a}
$$

Factoring:

Differences of Squares: $a^{2}-b^{2}=(a+b)(a-b)$


Step 1: Find the product (ac) $=10$
Step 2: Find the sum (b) $=7$

Step 3: Rewrite
5 an


Step 4: Factor out a GCF (work backwards to match)


Step 5: Write in factored form.

Factor by Grouping $2 x^{2}+7 x+5$


$$
\left(2 x^{2}+5 x\right)+(2 x+5)
$$



## Practice:

Find the vertex, $y$-intercept, $x$-intercept, line of symmetry, and tell if it opens up or down.

1. $y=-2 x^{2}+12 x-7$
2. $y=\frac{1}{4} x^{2}$
3. $y=4 x^{2}+7$
4. $y=-x^{2}-2 x-3$

Find the zero(s) of the equation.
5. $f(x)=x^{2}-2 x-3$
6. $h(x)=x^{2}+x+1$
7. $g(x)=x^{2}+6 x-7$
8. $k(x)=-x^{2}+6 x-9$

Solve the equation. Note some may require the Quadratic Formula.
9. $2 x^{2}=8$
10. $-10=r^{2}-10 r+12$
11. $3 x^{2}-11=7$
12. $4 z^{2}=9$
13. $7 c^{2}=100$
14. $3 x^{2}+5 x=8$
15. $2 x^{2}-7=x$
16. $3 g^{2}-6 g-14=3 g$
17. $6 z^{2}=2 z^{2}+7 z+5$
18. $-4 y^{2}-3 y+3=2 y+4$
19. $(x+13)^{2}=25$
20. $-2 x^{2}=-32$

